

# Write or Radiate: Inscribed Mass vs. Electromagnetic Channels

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## 10 Years of WINLAB Research (Infostations redux)

- **Infostations:**
  - Delay tolerant?  $\Rightarrow$  transmit when near base!
- **Channel Quality**
  - How good can that RF channel be?  $\Rightarrow$  really good!
- **Interference Avoidance, Pricing & Spectrum Management**
  - Interference hurts  $\Rightarrow$  deal with it!

## Completely ridiculous ..... right?

– Forget RF! Write message down! Toss it to recipient!

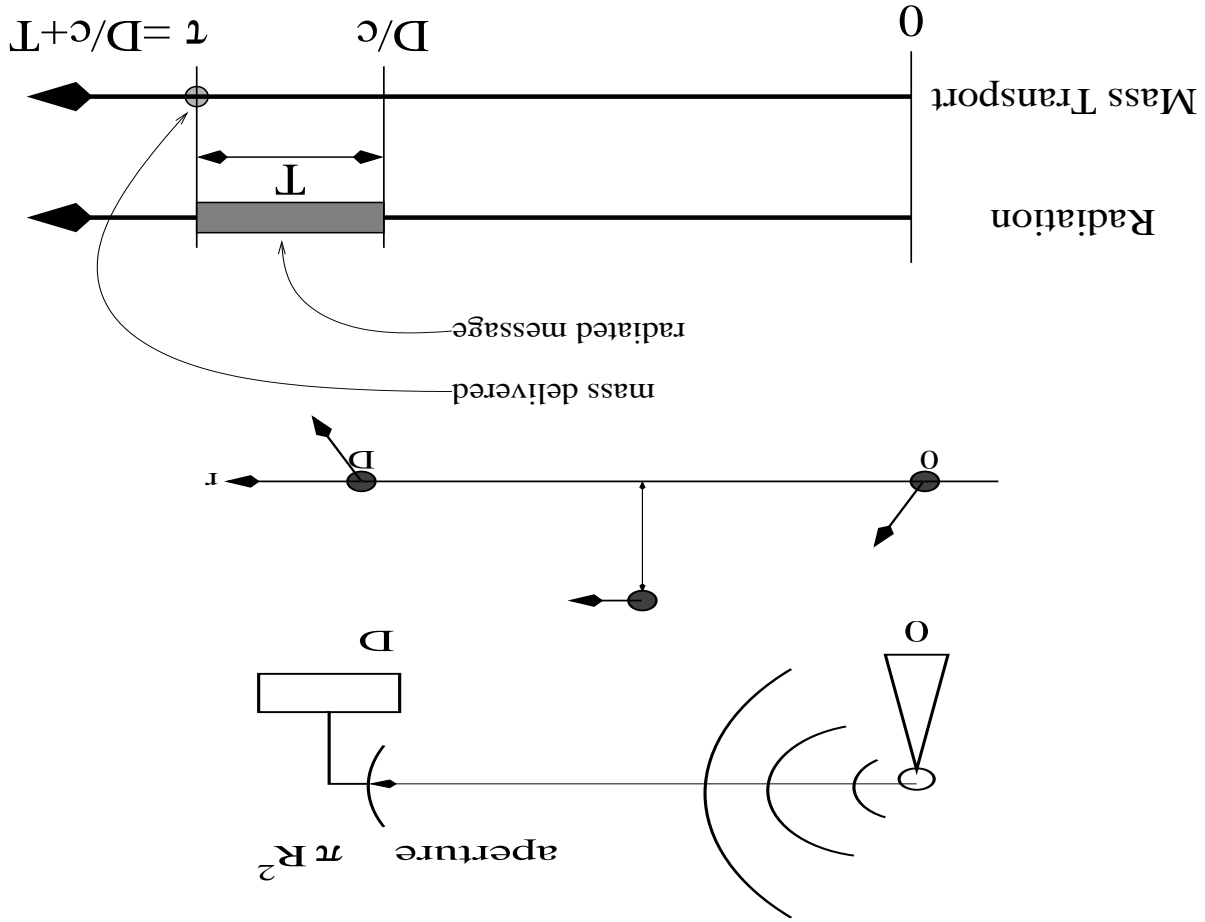
- IMPLICATION:
- Can tolerate delay
- Channel good when nearby
- Storage density is increasing
- RF Interference is bad

**A Hoary Old Epiphany!**

## A Little Empirical Rigor

- **Optical Lithography with SiO<sub>2</sub>**:  $3.85 \times 10^{18}$  bits/kg
- **E-beam Lithography with SiO<sub>2</sub>**:  $1.54 \times 10^{21}$  bits/kg
- **STM with Xe on Ni**:  $1.74 \times 10^{22}$  bits/kg
- **RNA**:  $1.8 \times 10^{24}$  bits/kg
- 1 bit per nm<sup>3</sup>  $\rightarrow$   $1\text{mm}^3 = 10^{18}$  bits!
- And maybe a LOT more room at the bottom

# A Little Analytic Rigor



## Parameters and Definitions

- $B$ : message size (bits).
- $\rho$ : mass information density for inscribed information (bits  $\text{kg}^{-1}$ ).
- $W$ : bandwidth available for radiated communication (Hz).
- $A = \pi R^2$ : effective receiver aperture ( $\text{m}^2$ ).
- $D$ : distance to receiver (m).
- $N_0$ : background noise energy ( $\text{W Hz}^{-1}$ ).
- $\tau$ : message deadline (s)
- $T$ : radio messaging time (s).
- $\delta = \frac{(D/\tau)}{c}$ : ratio of  $\tau$  to the light travel time.

## Rocket Science Foundations

- Max bigger than mean:

$$\max_v h(v) \geq E[h(V)]$$

- If  $V$  deterministic:

$$\max_v h(v) = E[h(V)]$$

- If  $h(\cdot)$  convex (Jensen):

$$E[h(V)] \geq h(\bar{v})$$

## Rocket Science

- Average velocity

$$\frac{1}{D} \int_0^{\tau} v(t) dt = \bar{v} = \frac{D}{E[v(t)]}$$

- Minimum imparted energy

$$E_* = \min_t h(v(t))$$

subject to  $\bar{v} = \frac{D}{\tau}$ .

- Jensen says

$$E_* = \min_t h(v(t)) \geq \min_{\bar{v}} E[h(v(t))] \geq h(\bar{v})$$

with equality iff  $v(t)$  is constant



## Minimum Transport Energy

- GIVEN:  $h(\bar{v})$  and  $\bar{v}$

$$E_* = h(\bar{v})$$

- $h(\bar{v}) = mc^2 \left( \frac{\sqrt{1 - \frac{\bar{v}^2}{c^2}}}{1} - 1 \right)$  :

$$E_* = mc^2 \left( \frac{\sqrt{1 - \left(\frac{\bar{v}}{c}\right)^2}}{1} - 1 \right)$$

- $h(\bar{v}) \approx \frac{1}{2}m\bar{v}^2$  :

$$E_* \approx \frac{1}{2}m\bar{v}^2$$

## Potential Fields

- $q(x)$  potential energy:

$$\mathcal{E}(t) = h(v(t)) + q(x(t))$$

- Energy minimization:

$$E_* = \min_t \max_x \mathcal{E}(t) \geq \min_t \int_0^1 \mathcal{E}(t) dt$$

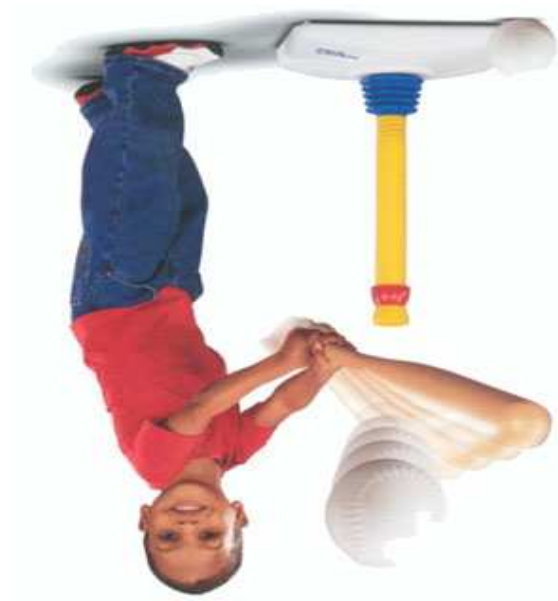
- Calculus of variations:

$$0 = \frac{d}{dt} \left( \frac{\partial \mathcal{E}}{\partial v} \right) - \frac{\partial \mathcal{E}}{\partial x}$$

$$0 = \ddot{x}h''(x) - p'(x)$$

## Potential Field Results

- Low speed:
- $m\ddot{x} = q'(x)$
- $q'(x)$  is force at position  $x$ :  $\rightarrow$  “free fall”
- Freefall?  $\rightarrow \mathcal{E}(t) = \text{constant}$
- $\mathcal{E}(t)$  constant  $\rightarrow$  minimization satisfied with equality, so ...



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- $\mathcal{E}(t)$  constant  $\rightarrow$  minimization satisfied with equality, so ...

## Potential Field Results

## Artillery Problem

- Minimum energy:

$$E_* = \frac{1}{2}mgD$$

- Let  $\delta = c\tau/D$ .

- Delay at minimum energy

$$\delta_* = c\sqrt{2/gD}$$

- Pay a factor of 2 over free space

## Escape Problem

- Needs numerical calculation
- Boils down to: need initial velocity larger than escape.
- About a factor of 2 energy penalty, again
- Escape examples (rough):
  - Earth:  $\delta > 2 \times 10^4$
  - Solar:  $\delta > 2 \times 10^3$
  - Milky Way:  $\delta > 6 \times 10^2$

## Inscribed Mass Energy Requirements

- Message size  $B$ , mass information density  $\tilde{\rho}$

- General

$$E_w = \frac{B}{\tilde{\rho}} c^2 \left( \frac{\sqrt{\delta^2 - 1}}{\delta} - 1 \right)$$

- $\delta \gg 1$ :

$$E_w \approx \frac{1}{2} \frac{B}{\tilde{\rho}} \left( \frac{\delta}{c} \right)^2$$

- Off by only  $\approx 10\%$  at  $0.4c$  and  $\approx 50\%$  at  $0.75c$

- Low speed ain't so low!

- Can (usually) ignore relativity

## Radiation Energy Requirements

- Energy capture (no gain yet):

$$v(D) = \frac{4\pi D^2}{A}$$

- Bits a la Shannon:

$$B = TC = TW \log_2 \left( \frac{PA}{4\pi D^2 N_0 W} + 1 \right)$$

- $E_r = PT$ ,

$$E_r = BN_0 \frac{4\pi D^2}{TW} \frac{A}{B} \left[ 2^{\frac{TW}{B}} - 1 \right]$$

- Large  $TW$ :

$$E_r \geq BN_0 \frac{4\pi D^2}{A} \ln 2$$



$$\Omega \geq \left[ \frac{\tilde{p}_{N_0}}{c^2} \right] \left[ \frac{4\pi D^2}{A} \right] (2 \ln 2) \delta^2$$

- Large bandwidth  $W$ ,  $\delta \gg 1$

$$\Omega = \frac{E_r}{E_w}$$

- Definition:

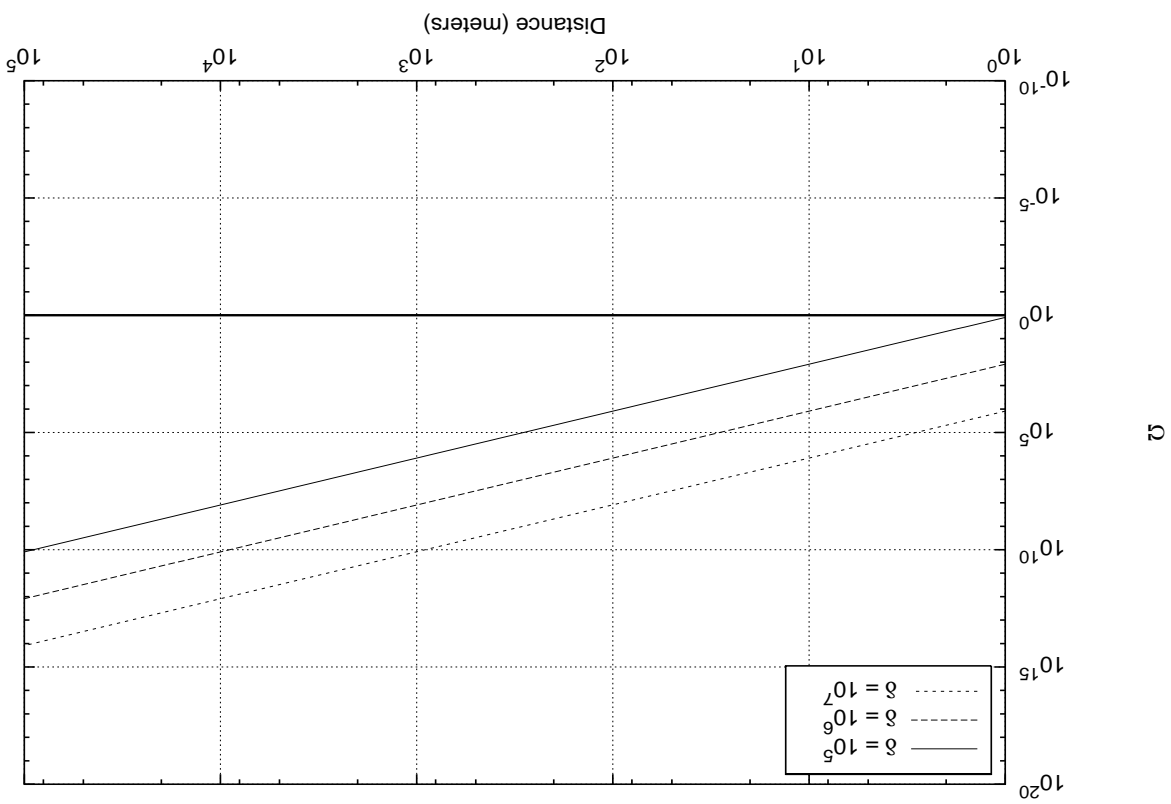
**Radiation to Transport Energy Ratio**

## What About Gain?

- Gain:  $G_{\max} = \frac{8\pi^2 R^2}{\lambda^2}$
- Critical  $p$ :  $p_* = \arg p \left\{ \frac{E_r(G)}{E_w(p)} = 1 \right\}$
- $p_*$  for  $\lambda = 0.03m$ :

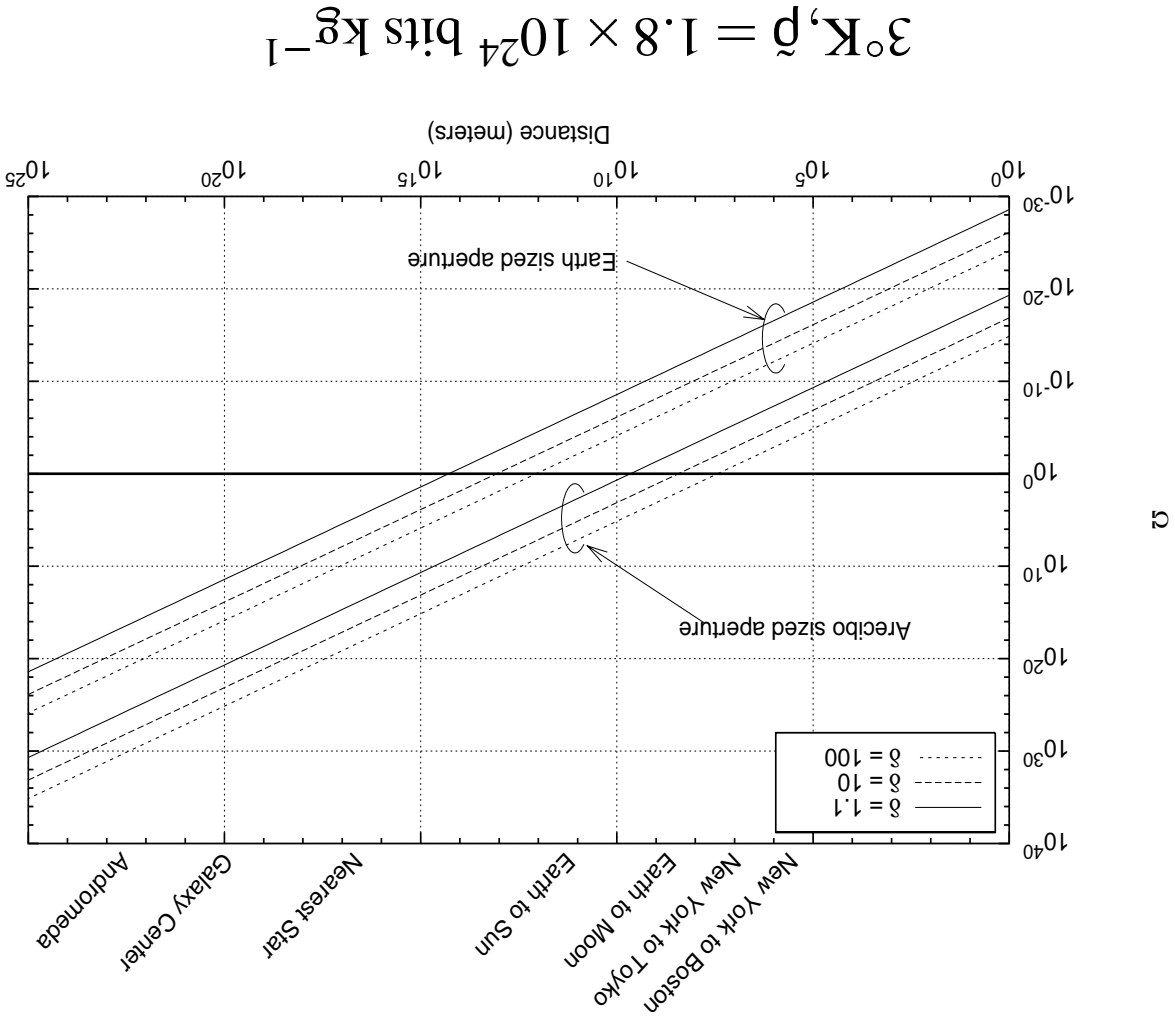
Aperture	$p_*$	Far Field
(0.05 m)	$2.15 \times 10^{36} \left[ \frac{D\delta}{\text{I meter}} \right]^{-2} \frac{\text{bits}}{\text{kg}}$	$D = 0.37 \text{ m}$
(Arecibo)	$1.95 \times 10^{20} \left[ \frac{D\delta}{\text{I light year}} \right]^{-2} \frac{\text{bits}}{\text{kg}}$	$D \approx 3 \times 10^{-10} \text{ LY}$
(Earth)	$6.38 \times 10^{38} \left[ \frac{D\delta}{\text{I light year}} \right]^{-2} \frac{\text{bits}}{\text{kg}}$	$D \approx 0.6 \text{ LY}$

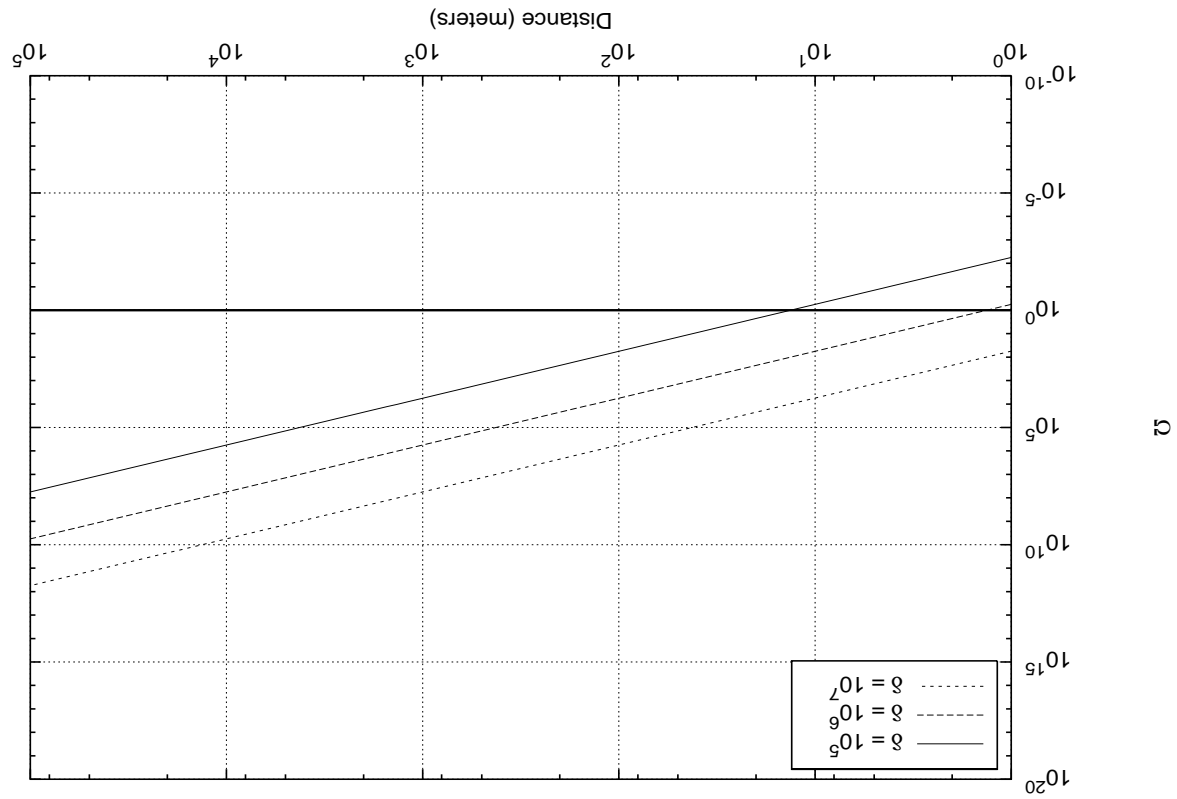
0.05m receive aperture radius,  $300^\circ\text{K}$ ,  $\rho = 1.8 \times 10^{24}$  bits  $\text{kg}^{-1}$



**Ω vs. Distance: point to point no gain**

# Ω vs. Distance: point to point no gain

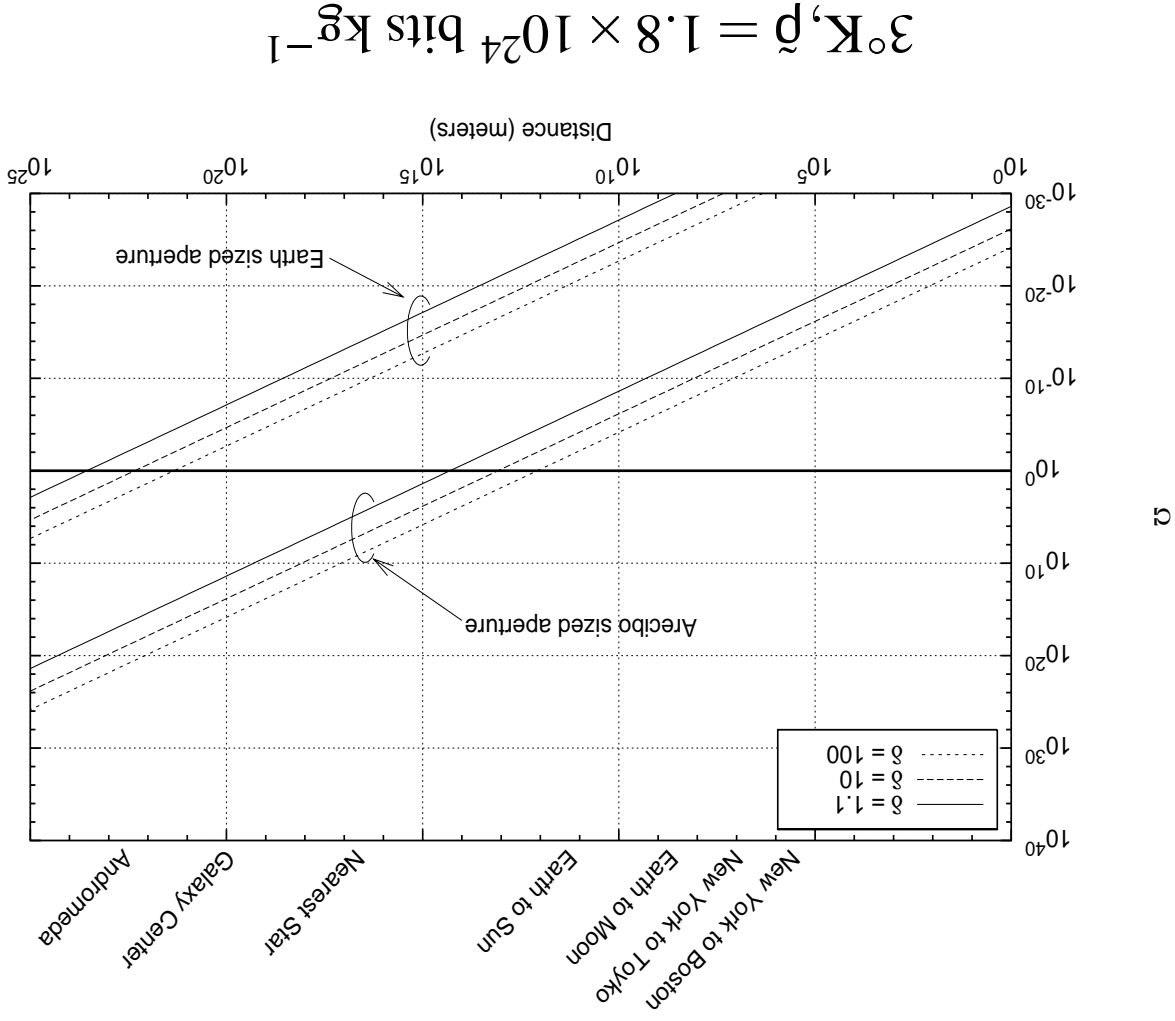




0.05m receive aperture radius,  $300^\circ\text{K}$ ,  $\rho = 1.8 \times 10^{24}$  bits  $\text{kg}^{-1}$

**Q vs. Distance: point to point with gain**

# Ω vs. Distance: point to point with gain

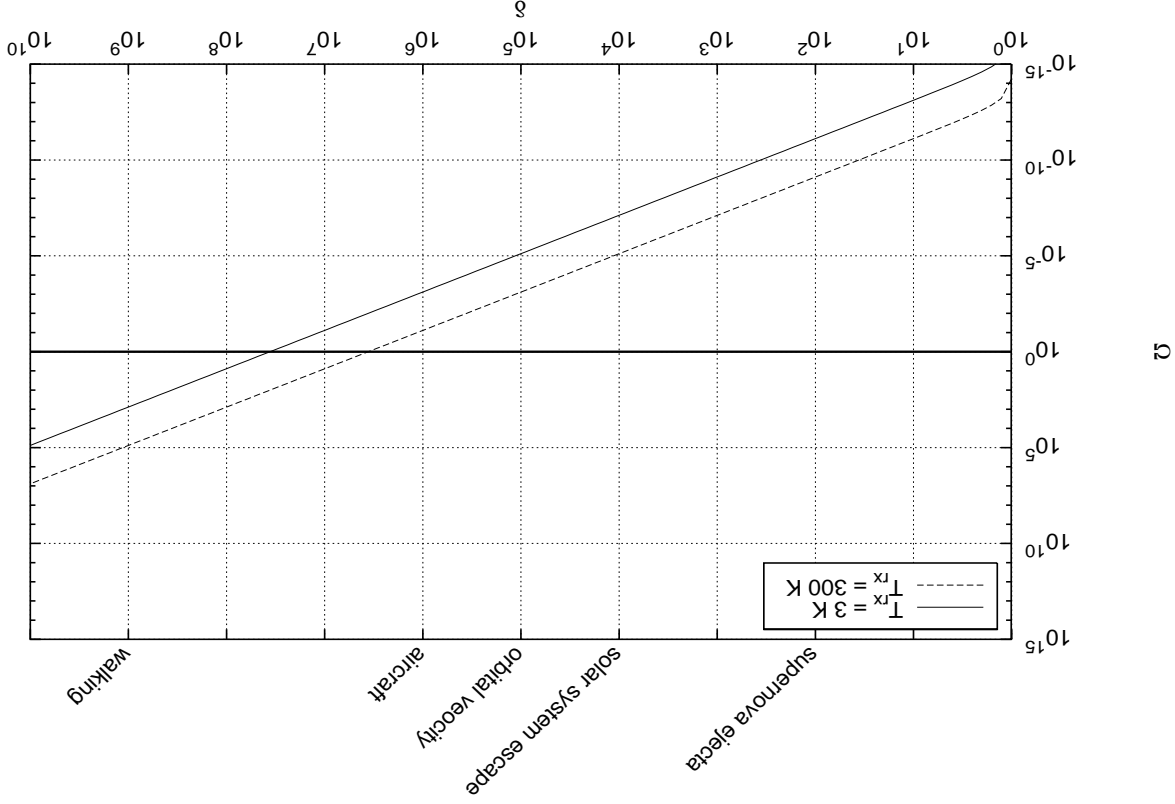


$$3^\circ K, \tilde{\rho} = 1.8 \times 10^{24} \text{ bits kg}^{-1}$$

## What About Broadcast?

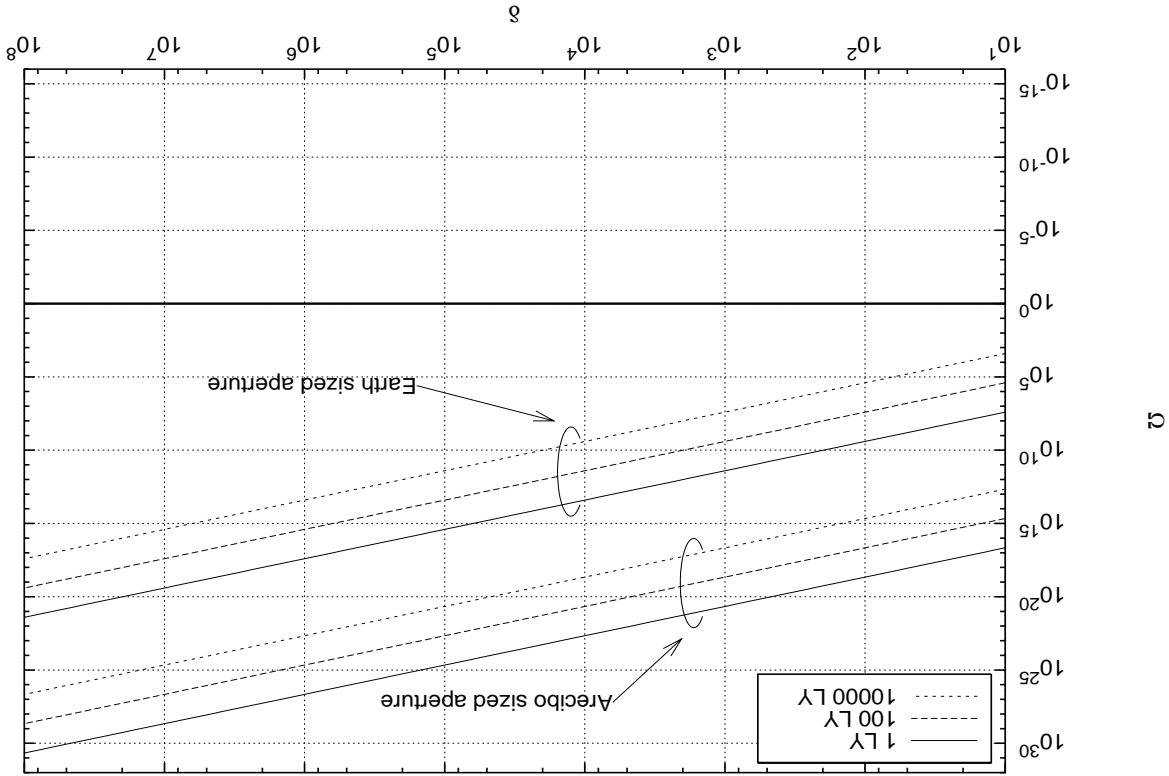
- Blind Broadcast
  - one message, many receivers, unknown positions
- Directed Broadcast
  - one message, many receivers, known positions
- Multicast
  - different messages, different receivers
  - large BW limit: separate radiative channels (essentially pt2pt)

# One Message, Unknown Locations



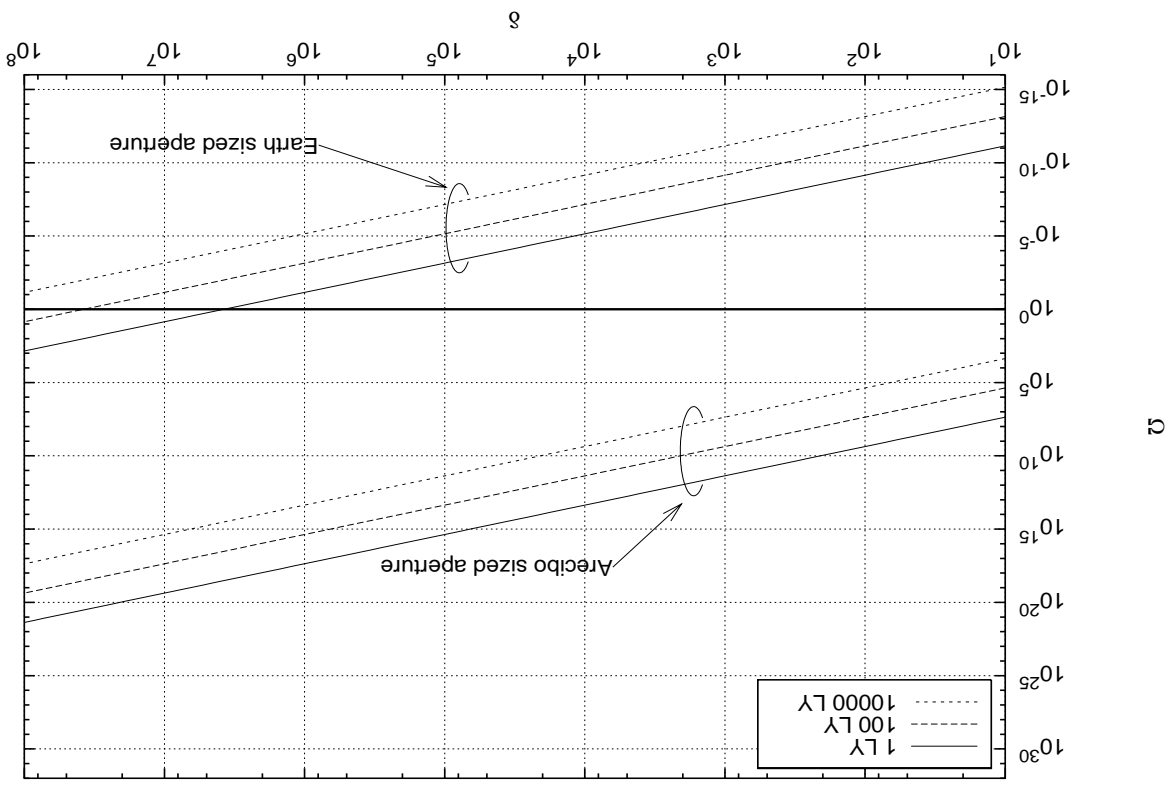


# One Message, Known Locations, No Gain: interstellar



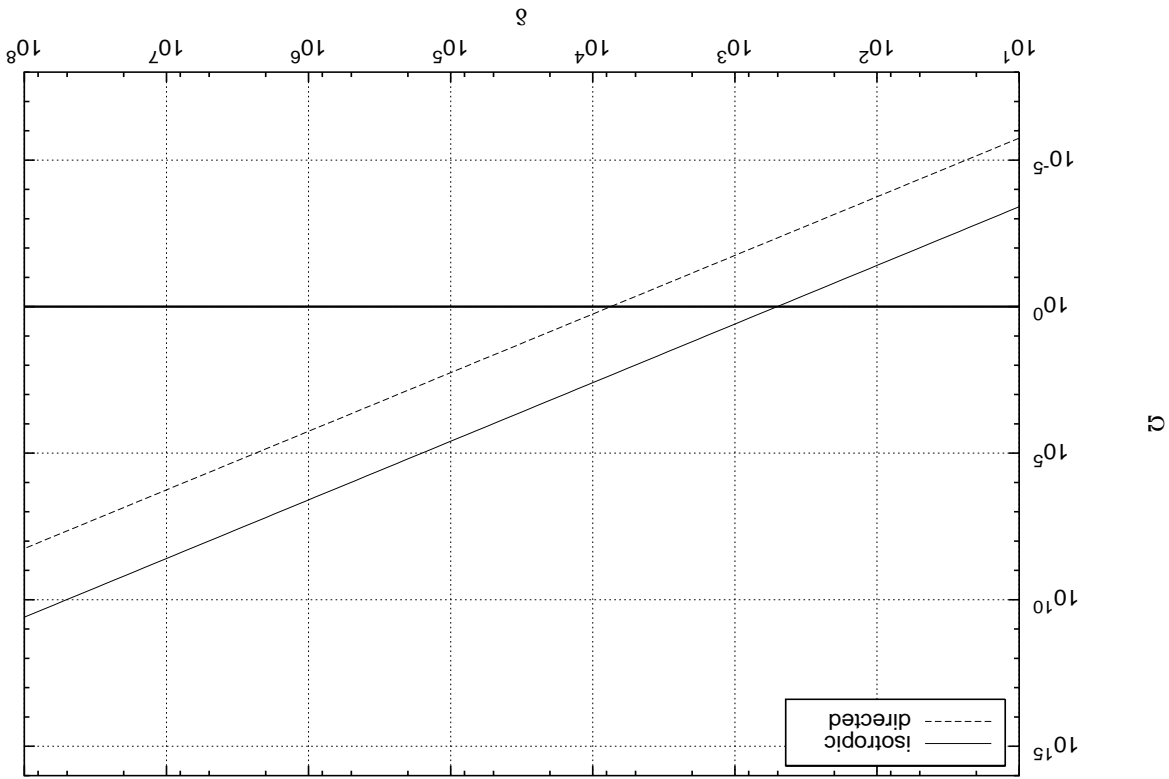
Energy ratio vs.  $\delta$ .  $\bar{p} = 1.8 \times 10^{24}$  bits  $\text{kg}^{-1}$ ,  $3^\circ\text{K}$ , receiver density  $\sigma = 6.4 \times 10^{-3}$  light year $^{-3}$  (stellar density of Milky Way).

# One Message, Known Locations with Gain: interstellar



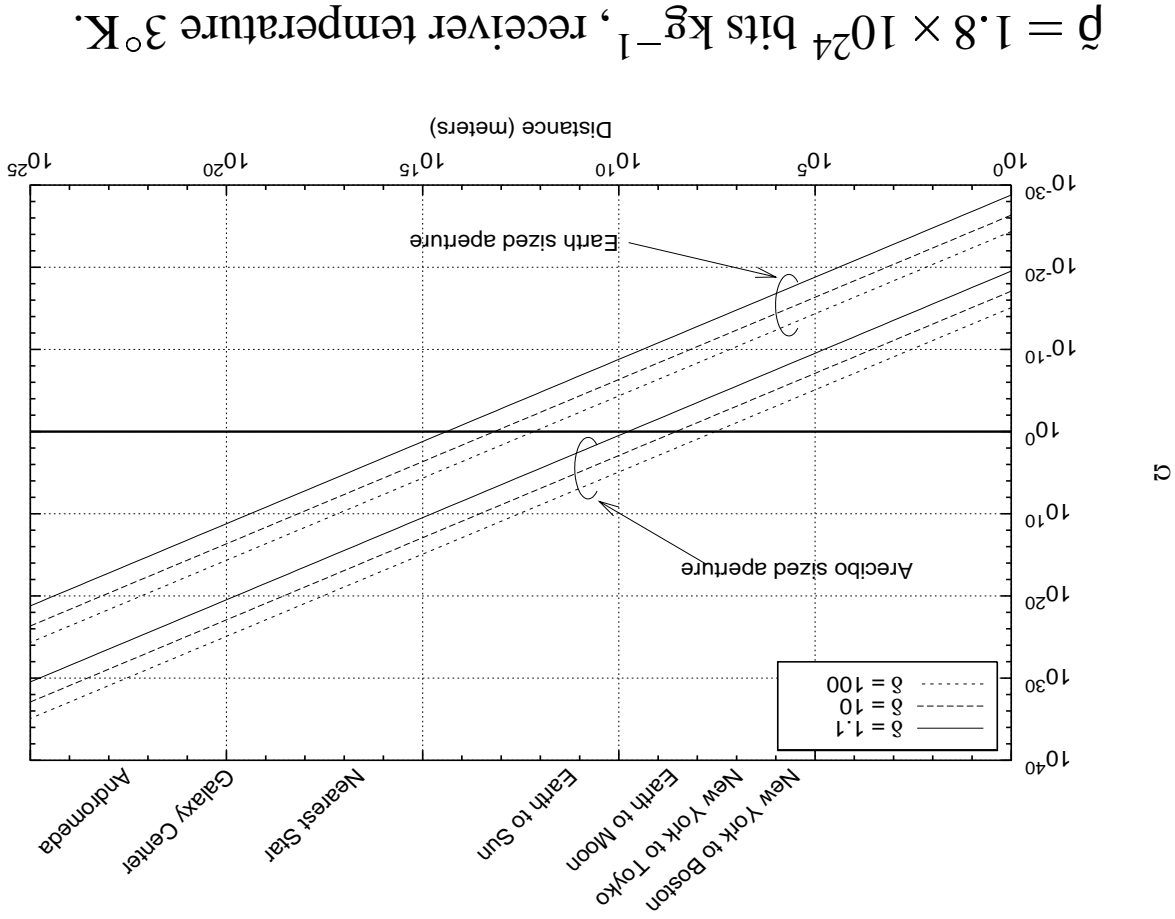
Same but with gain.

Energy ratio vs.  $\delta$ .  $\beta = 1.8 \times 10^{24}$  bits  $\text{kg}^{-1}$ ,  $300^\circ\text{K}$ , receiver aperture radius 0.05 m, receiver density  $\sigma = 0.01 \text{ m}^{-2}$ .

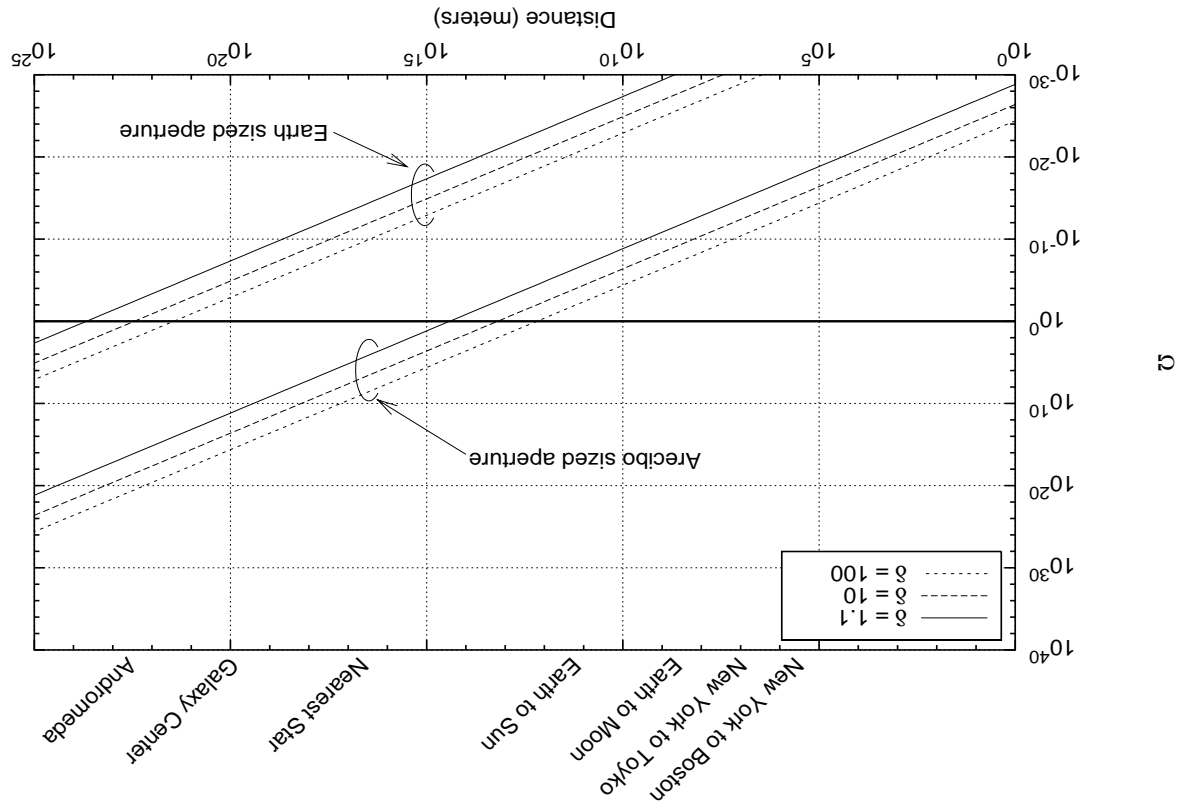


# One Message, Known Locations: terrestrial

# Many Messages, No Gain: interstellar

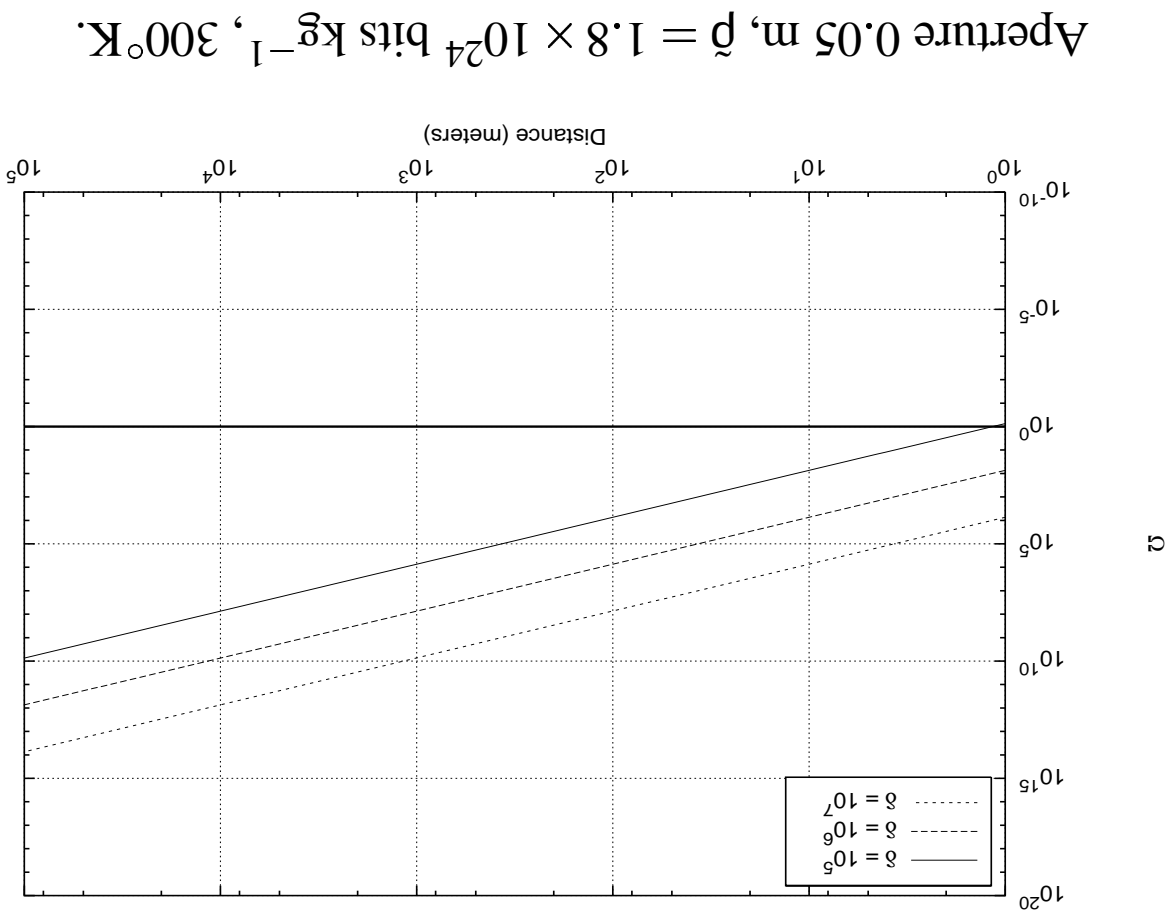


# Many Messages with Gain: interstellar

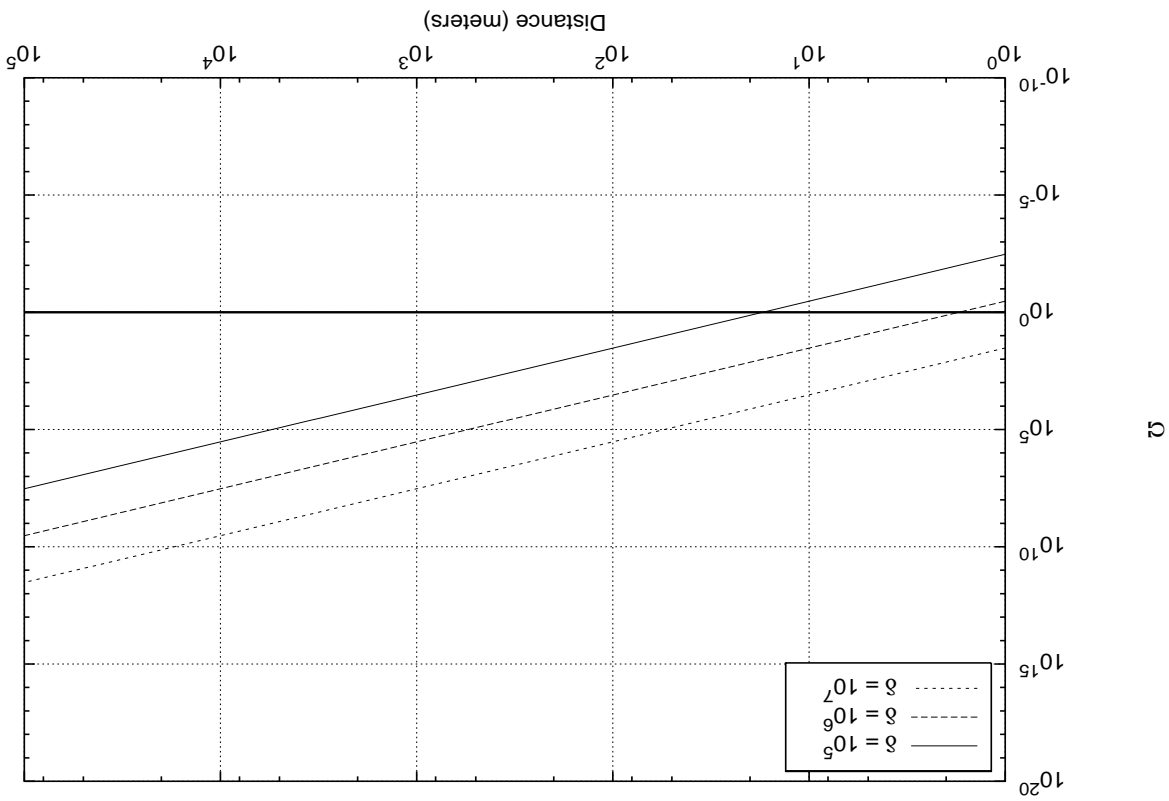


Same but with gain.

# Many Messages, No Gain: terrestrial



# Many Messages with Gain: terrestrial



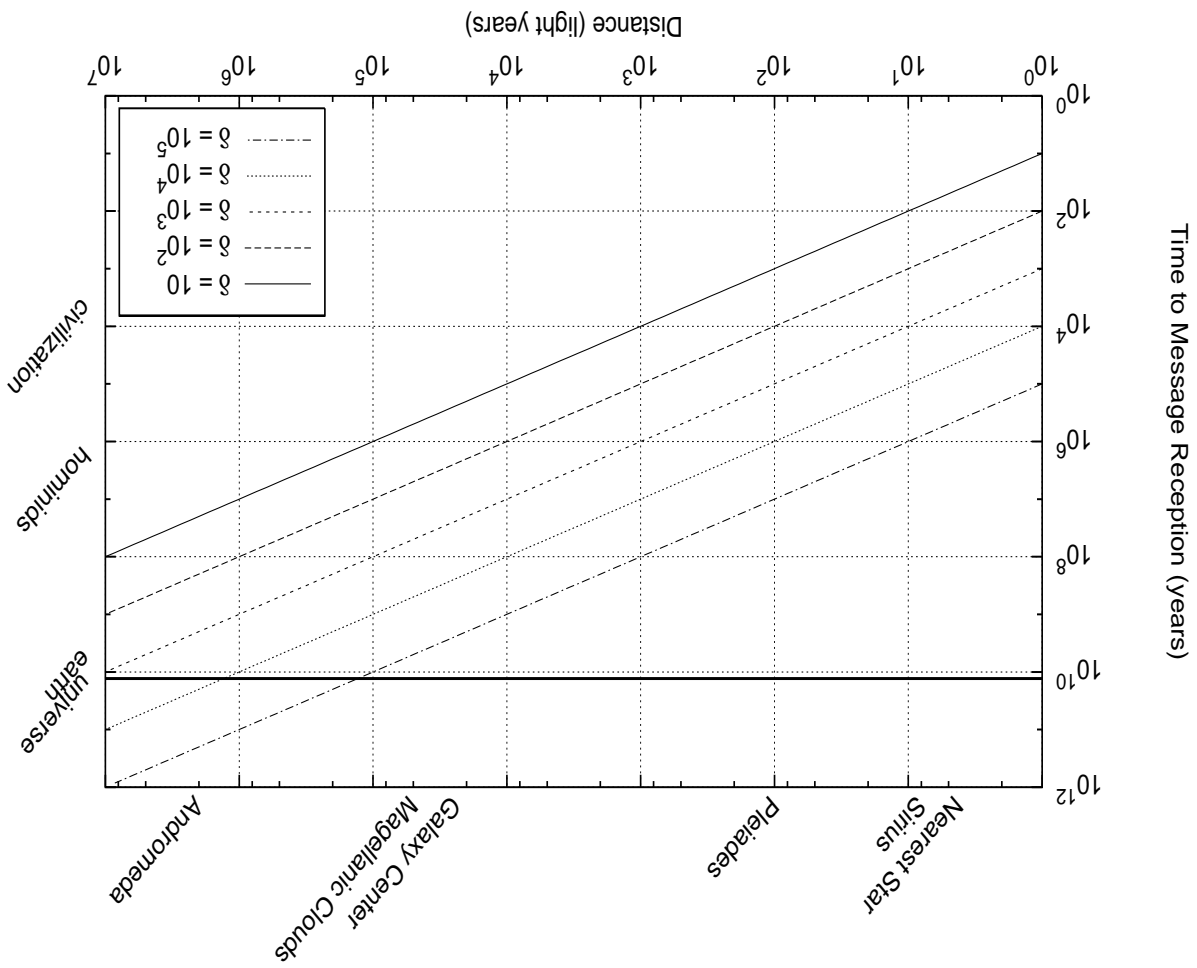
Same but with gain.

## Inscription Energy/Speed Issues

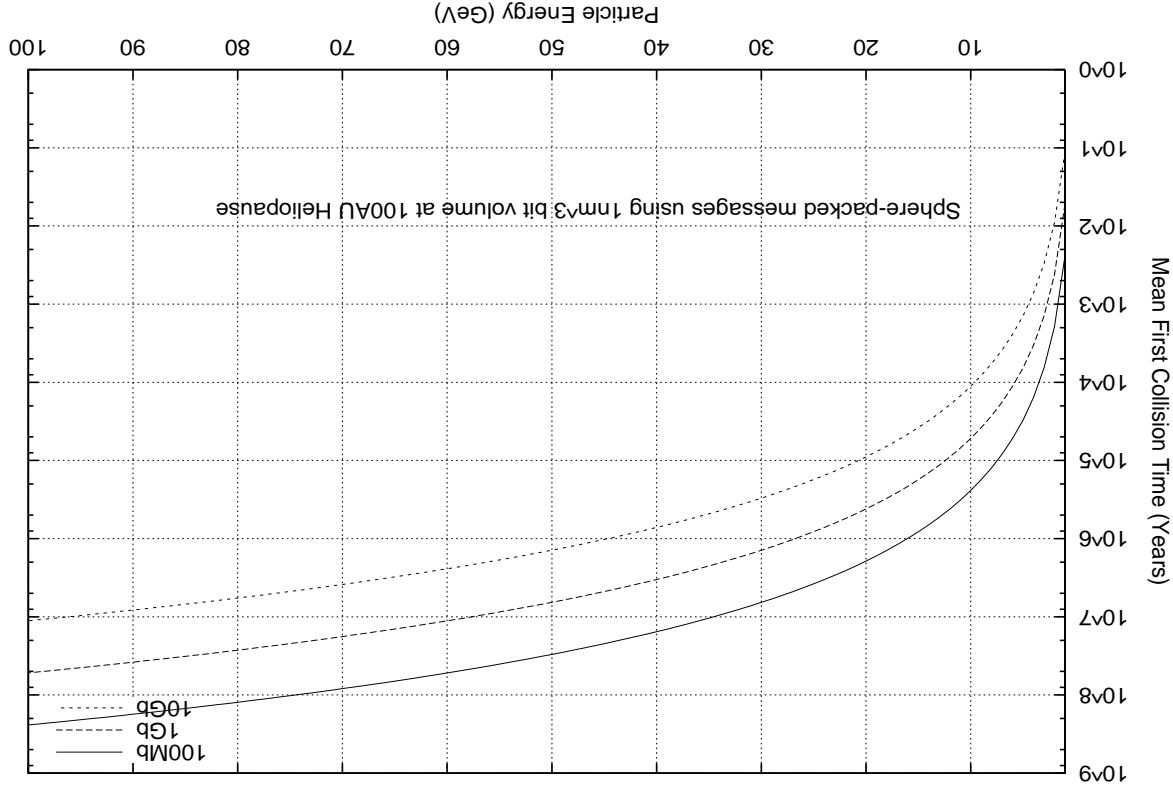
- **Mass Inscription/Readout Energy**
  - Landauer said it can be reversible
- **Mass Inscription/Readout Time**
  - Landauer said it can be arbitrarily fast
- **Empirical energy calc:**
  - 60000 ATP/second for 20 minutes: 4850 Kbase of E-coli
  - $8 \times 10^{-20}$  J per ATP
  - Replication:  $\approx 10^{-17}$  J bit<sup>-1</sup>
  - $E^*$  at  $\delta = 100$ :  $2.5 \times 10^{-12}$  J bit<sup>-1</sup>
  - CAVEAT:  $E^*$  goes down as  $\delta^{-2}$



# Delivery Times



# Message Integrity – High Energy Insults



## Damage Mechanisms

- Large (or small) unseen obstacles
- Heating (diffusion)
- Ion tracks
- Dislocation
- Spallation

## Hard to Speculate (so won't ... yet)

- Big rock?
- Dust?
- Embedded dust (comet)?
- Probe (Bracewell)
- Onward toward lunatic fringe

**Delivery Methods**

## Epiphany Revisited, Just for Fun!

- Gallon of gasoline:  $1.2 \times 10^8$  joules
- 20 miles/gallon
- 20 miles:  $1.2 \times 10^8$  joules
- $D^4$  isotropic breakeven ( $1\text{m}^2$  radius aperture):  $\approx 10^{10}$  bits
- $5.5 \times 10^{-12}$  grams of RNA
- 0.5 kg of 20 lb paper at 600 dots/inch

**The epiphany is REAL even for inefficient delivery!**

## PUNCHLINES

- Incribed mass messaging is NOT ridiculous
- Incribed mass messaging might often be PREFERRED
- Network Issues
  - Pebbles are non-interfering
  - Pebble net throughput scales well
  - Delays reasonable (Boston/NYC:  $\approx 270$  seconds ballistically)
- Practical value
  - Terrestrial: maybe some, maybe none
  - Interstellar: dust/pebbles/rocks, not spectrum for SETI
- Learn more: <http://www.winlab.rutgers.edu/~crose/cgi-bin/cosmic.html>